

Emergent Higgs

Ryuichiro Kitano (KEK, Sokendai)

collaboration with Yuichiro Nakai (Harvard)

126GeV

What is the **microscopic physics** behind the Higgs mechanism?

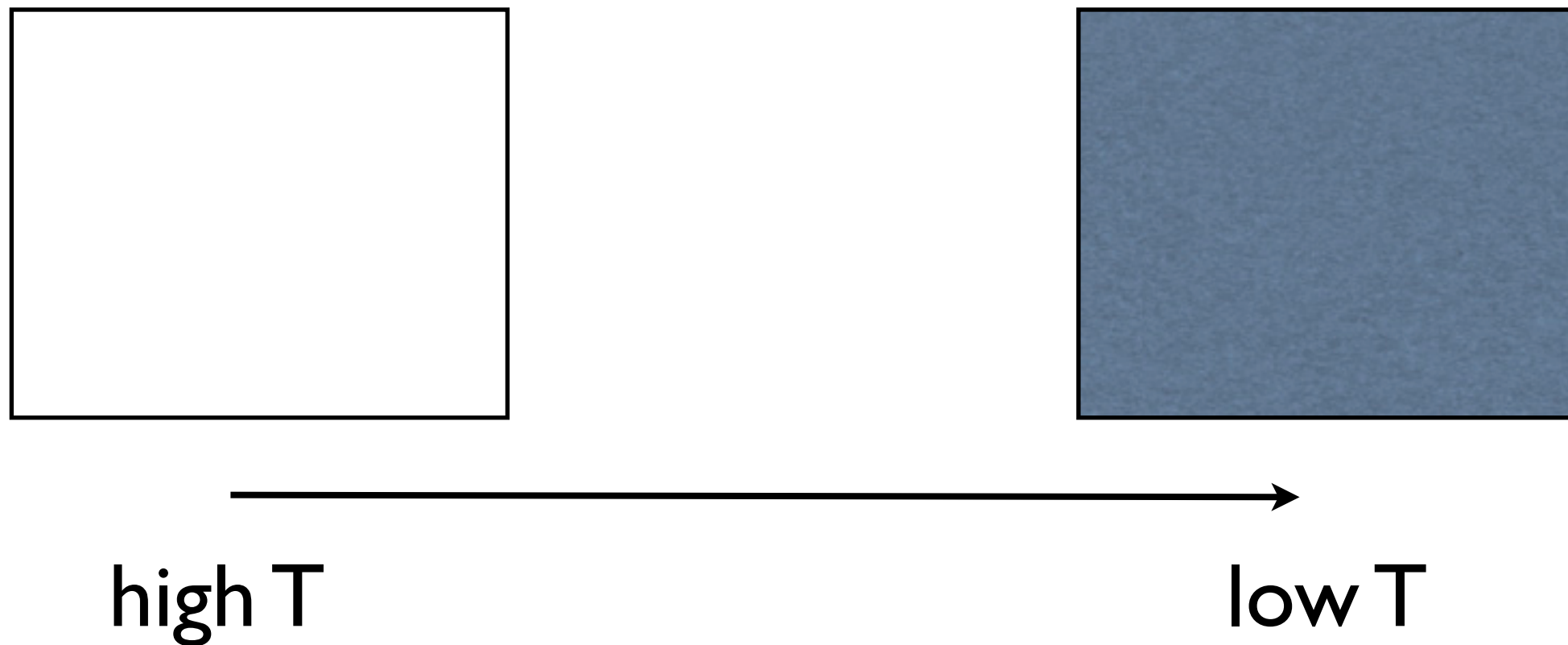
We know that

- EWSB happened **twice**: one by Higgs and another by QCD (chiral symmetry breaking).

There may be a unified framework to understand this.
(Higgs as a part of QCD?)

What's Higgs?

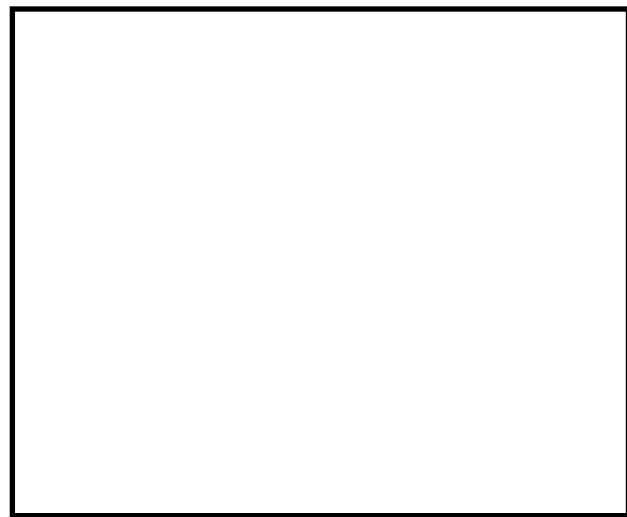
It is pretty similar to superconductivity.



But the theory is just QED.

What's Higgs?

another example: chiral symmetry breaking



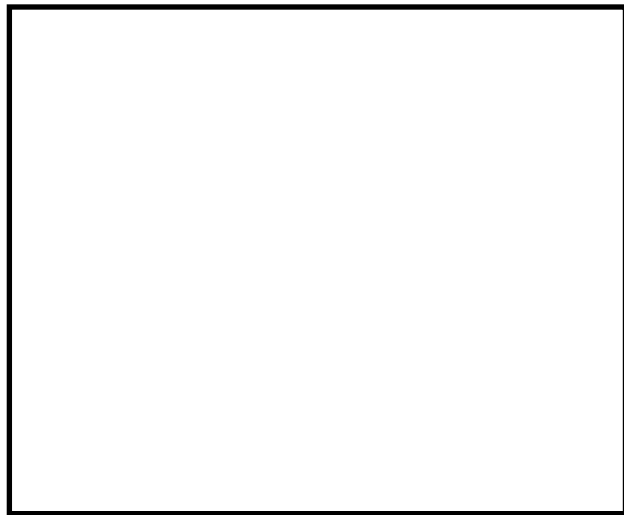
weak coupling

strong coupling

But the theory is just QCD.

hypothesis

Extra dimensional QCD



large extra dim.

small extra dim.

the theory is just QCD

Scenario

Standard Model in extra dim. (no Higgs)



compactification
+ non-perturbative effects
of SM gauge interactions

Standard Model (with Higgs)

“Self-breaking”

[Dobrescu '98][Cheng, Dobrescu, Hill '99][Arkani-Hamed, Dimopoulos '98]
[Arkani-Hamed, Cheng, Dobrescu, Hall '00]

Extra dimensional gauge theory?

5-dimensional gauge theory:

two parameters: g_5, R $\dim(g_5) = -1/2$

→ cut-off scale $\Lambda = \frac{8\pi^2}{g_5^2}$

large extra dim.

$$\frac{1}{R} \ll \Lambda$$

= weakly coupled

→ We get a weakly coupled
4D effective theory

$$\frac{1}{g_4^2} = \frac{2\pi R}{g_5^2} = \frac{R\Lambda}{4\pi} \gg \frac{1}{4\pi}$$

small extra dim. or high energy

$$\frac{1}{R} \gg \Lambda \quad \text{or} \quad E \gg \Lambda$$

= strongly coupled

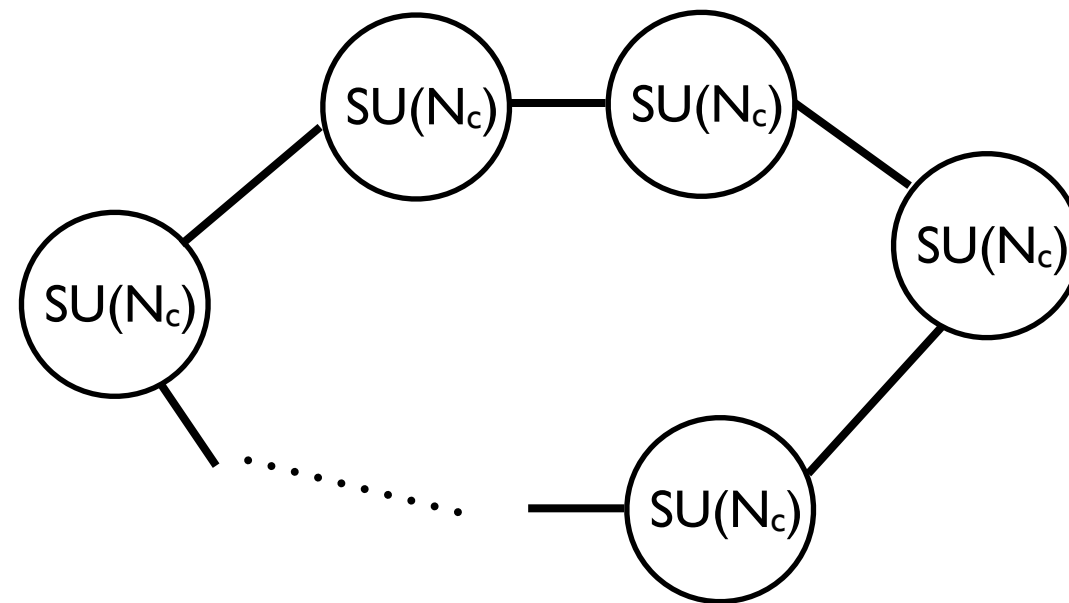
→ “???” (non-perturbative)

We hope “???” is going to be our Higgs.

We need a **definition** of the theory to discuss this region.
(results depend on how we cut off the theory..)

A (possible) definition of extra dim. theory

It has been
proposed that



provides a **UV completion**.

[Arkani-Hamed, Cohen, Georgi '01]

[Hill, Pokorski, Wang '01][Cheng, Hill, Pokorski, Wang '01]

Usual story: mimics extra-dimension only at low energy

N-site model: $\frac{1}{R} = \frac{4\pi g v}{N}, \quad \Lambda = \frac{(4\pi)^2 v}{g} \quad \Lambda_{\text{dec.}} \equiv \frac{N}{R} = 4\pi g v$

g : gauge coupling at each site, v : vev of the link fields



The $N \rightarrow \infty$ limit while fixing R and Λ means

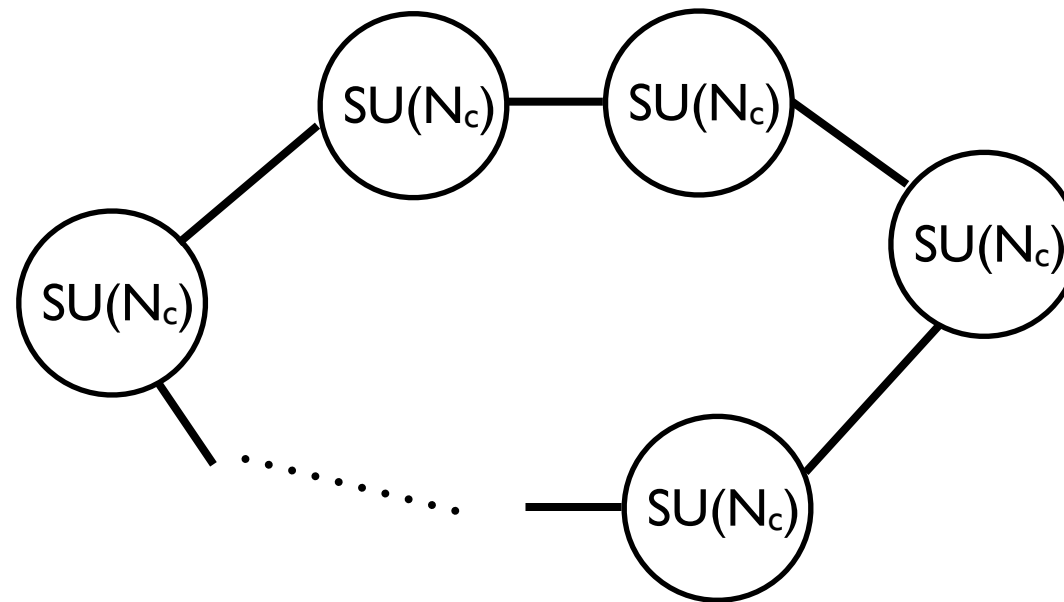
$$g \rightarrow \infty, \quad v \rightarrow \infty$$

But, we cannot go beyond $g \gg 1$.

→ One cannot take the continuum limit.

→ Equivalent to say that **we cannot discuss physics beyond the scale Λ** since $\Lambda > \Lambda_{\text{dec.}}$

But with $N=2$ SUSY,

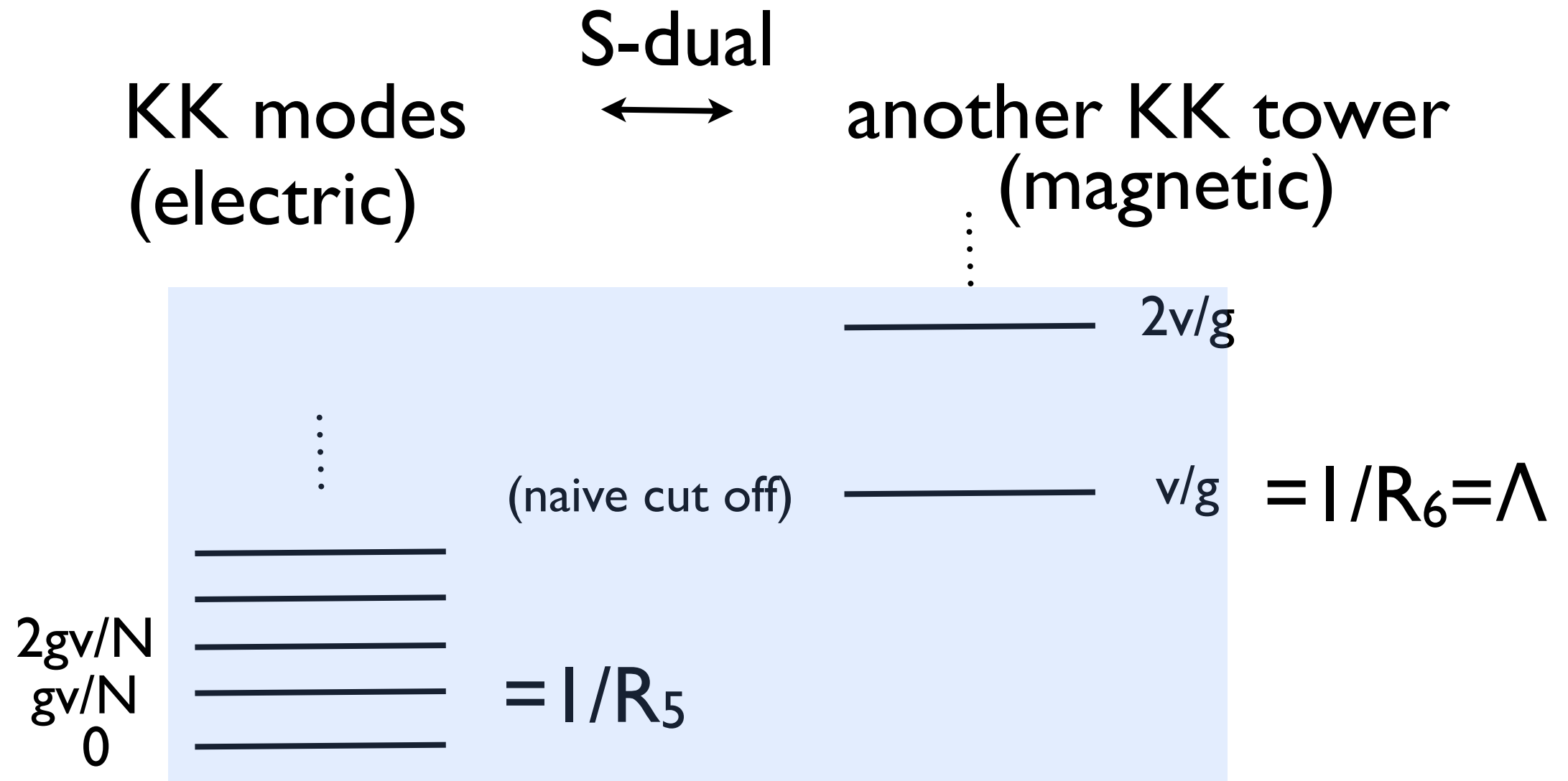


— $SU(N_c)$ — each site is a finite theory.
($N_f=2N_c$)

→ no problem with a large g .

→ We can go beyond Λ !!

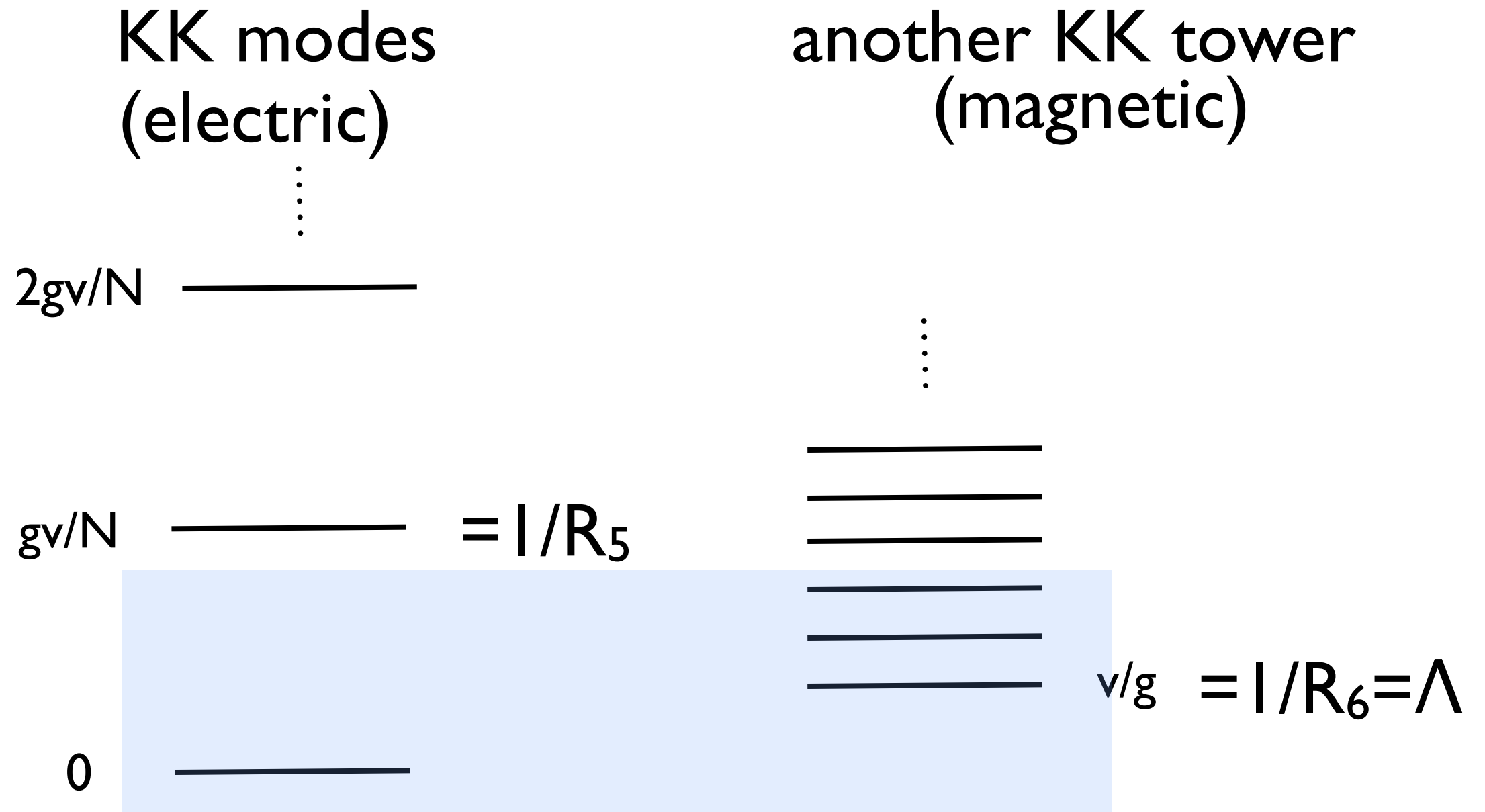
6th dimension



appearance of 6th dimension

Interesting.

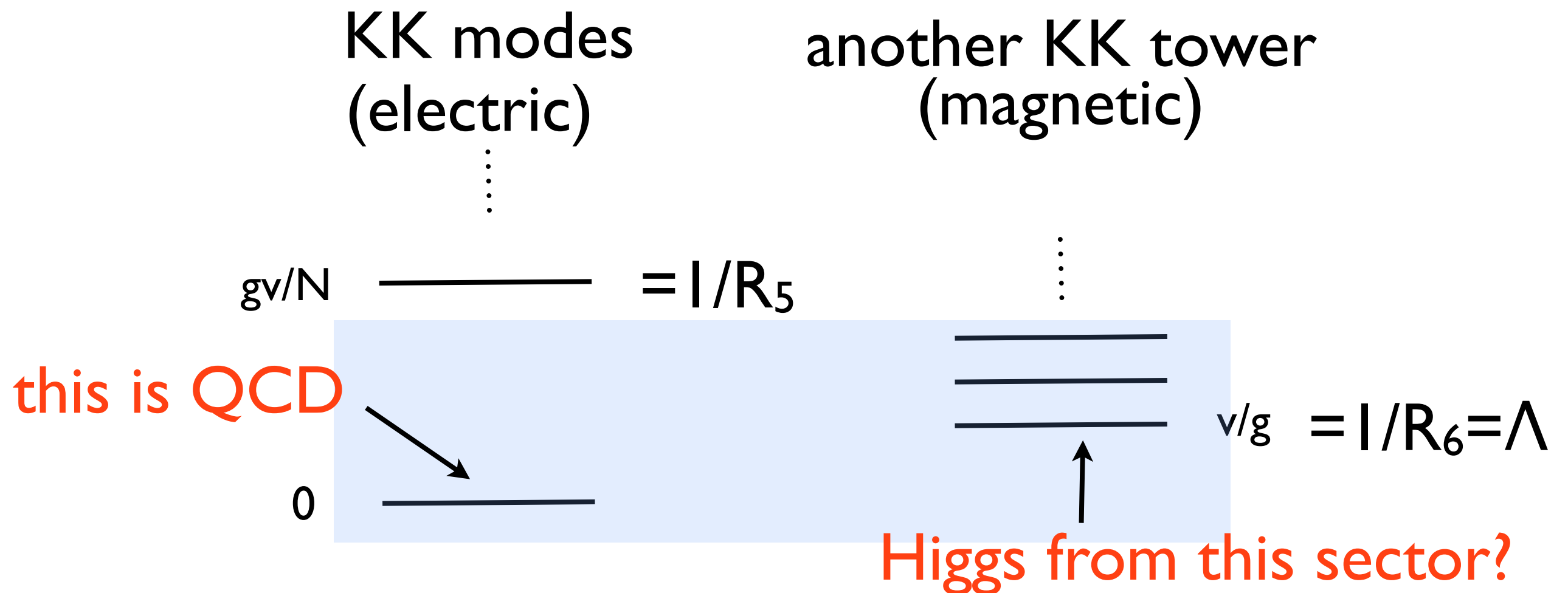
$1/R_5 \gg \Lambda$ means,
(small extra dim.)



magnetic picture gets better description.

Emergent Higgs

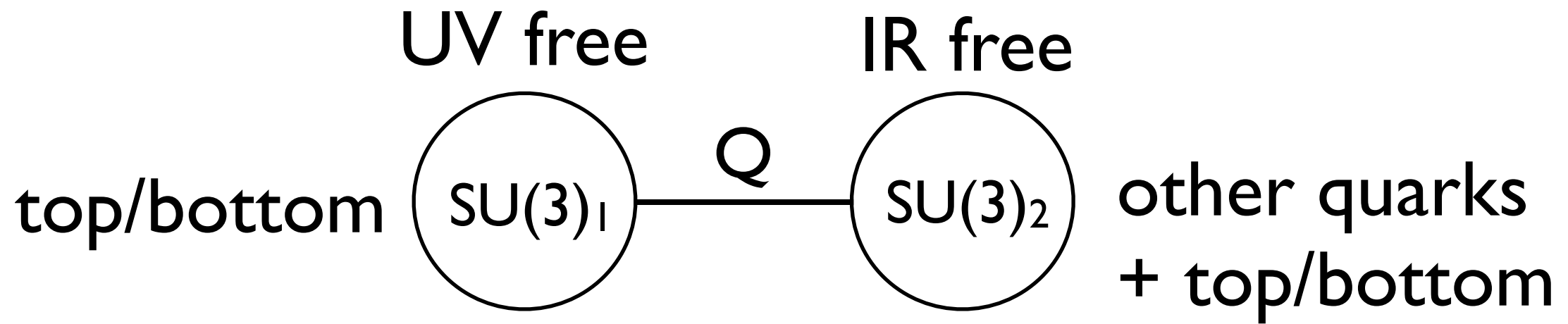
Higgs may be in the emergent degrees of freedom.



That would be an interesting unification.

a toy model: 2-site model

[RK, Nakai '12]



N=2
structure

	$SU(3)_1$	$SU(3)_2$	$U(1)_B$	$SU(2)_L \times U(1)_Y$
Q	3	$\bar{3}$	1	1_0
\bar{Q}	$\bar{3}$	3	-1	1_0
Φ	1	1 + 8	0	1_0
q_1	3	1	1	$2_{1/6}$
t_1^c	$\bar{3}$	1	-1	$1_{-2/3}$
b_1^c	$\bar{3}$	1	-1	$1_{1/3}$
q_2	1	3	0	$2_{1/6}$
t_2^c	1	$\bar{3}$	0	$1_{-2/3}$
b_2^c	1	$\bar{3}$	0	$1_{1/3}$
\bar{q}_2	1	$\bar{3}$	0	$\bar{2}_{-1/6}$
\bar{t}_2^c	1	3	0	$1_{2/3}$
\bar{b}_2^c	1	3	0	$1_{-1/3}$

Topcolor model [Hill '91]
[RK, Fukushima, Yamaguchi '10]
([Craig, Stolarski, Thaler '11][Csaki, Shirman,
Terning '11][Cohen, Hook, Torroba '12][Evans,
Ibe, Yanagida '12]...)

gauged
(Lagrange multiplier)
($\langle Q \rangle = v$ is fixed)

no Higgs field

$$W = \sqrt{2}g (q_1 \bar{Q} \bar{q}_2 + t_1^c Q \bar{t}_2^c + b_1^c Q \bar{b}_2^c + \bar{Q} \Phi Q - v^2 \text{Tr} \Phi + v_q \bar{q}_2 q_2 + v_t \bar{t}_2^c t_2^c + v_b \bar{b}_2^c b_2^c).$$

KK modes

For $\Lambda_1 \ll 4\pi v$ (weak coupling)

$$SU(3)_1 \times SU(3)_2 \longrightarrow SU(3)_{1+2}$$

We get MSSM **without Higgs** as low energy theory.

Below, we study the case with

$$\Lambda_1 \gg 4\pi v \quad (\text{strongly coupled region})$$

→ we will see that magnetic degrees of freedom appear.

Seiberg duality [Seiberg '94]

$SU(3)_1$ factor gets strong

→ weakly coupled magnetic picture (CFT)

Higgs appeared.

	$SU(3)_1$	$SU(3)_2$	$U(1)_B$	$SU(2)_L \times U(1)_Y$
Q	3	$\bar{3}$	1	1_0
\bar{Q}	$\bar{3}$	3	-1	1_0
Φ	1	$1+8$	0	1_0
q_1	3	1	1	$2_{1/6}$
t_1^c	$\bar{3}$	1	-1	$1_{-2/3}$
b_1^c	$\bar{3}$	1	-1	$1_{1/3}$
q_2	1	3	0	$2_{1/6}$
t_2^c	1	$\bar{3}$	0	$1_{-2/3}$
b_2^c	1	$\bar{3}$	0	$1_{1/3}$
\bar{q}_2	1	$\bar{3}$	0	$\bar{2}_{-1/6}$
\bar{t}_2^c	1	3	0	$1_{2/3}$
\bar{b}_2^c	1	3	0	$1_{-1/3}$



	$SU(2)_1$	$SU(3)_2$	$U(1)_B$	$SU(2)_L \times U(1)_Y$
f	2	1	$3/2$	2_0
\bar{f}_u	$\bar{2}$	1	$-3/2$	$1_{1/2}$
\bar{f}_d	$\bar{2}$	1	$-3/2$	$1_{-1/2}$
H_u	1	1	0	$2_{1/2}$
H_d	1	1	0	$2_{-1/2}$
f'	2	3	$3/2$	$1_{1/6}$
\bar{f}'	$\bar{2}$	$\bar{3}$	$-3/2$	$1_{-1/6}$
q	1	3	0	$2_{1/6}$
t^c	1	$\bar{3}$	0	$1_{-2/3}$
b^c	1	$\bar{3}$	0	$1_{1/3}$

below the dynamical scale Λ_1 .

weakly coupled

a-maximization gives

[Intriligator, Wecht '03]

$$D(H_d) = 1.03, \quad D(H_u) = 1.13, \quad D(q) = 1.13, \quad D(t^c) = 1.17,$$

$$D(f) = 0.99, \quad D(\bar{f}_u) = 0.99, \quad D(\bar{f}_d) = 0.88, \quad D(f') = 0.84, \quad D(\bar{f}') = 0.88.$$

$$\longrightarrow \frac{\tilde{g}}{4\pi} \sim 0.41, \quad \frac{\lambda_d}{4\pi} \sim 0.11, \quad \frac{\lambda_u}{4\pi} \sim 0.26, \quad \frac{\lambda_t}{4\pi} \sim 0.29, \quad \frac{\lambda_q}{4\pi} \sim 0.26,$$

(we assumed $\lambda_b \ll 4\pi$ by taking small v_b)

$$W = \lambda_d \bar{f}_u H_d f + \lambda_u \bar{f}_d H_u f + \lambda_t \bar{f}_u t^c f' + \lambda_b \bar{f}_d b^c f' + \lambda_q \bar{f}' q f + \frac{(4\pi v)^2}{\Lambda_1} \bar{f}' f',$$
$$= \Lambda'$$

$$\Lambda_1 \gg 4\pi v \longrightarrow \Lambda' \ll 4\pi v \quad (\text{appearance of light degrees of freedom})$$

below Λ'

Partially composite Higgs
[RK, Luty, Nakai '12]

$$W = \lambda_d \bar{f}_u H_d f + \lambda_u \bar{f}_d H_u f - \frac{\lambda_q \lambda_t}{\Lambda'} f \bar{f}_u t^c q - \frac{\lambda_q \lambda_b}{\Lambda'} f \bar{f}_d b^c q.$$

$SU(2)_I$ factor confines

(note: at this stage, λ 's get renormalized by $O(1)$ factors.)

$$\longrightarrow W = \frac{\lambda_u \Lambda'}{4\pi} H_u H'_d + \frac{\lambda_d \Lambda'}{4\pi} H_d H'_u - \frac{\lambda_q \lambda_t}{4\pi} H'_u t^c q - \frac{\lambda_q \lambda_b}{4\pi} H'_d b^c q.$$

	$SU(3)_2$	$U(1)_B$	$SU(2)_L \times U(1)_Y$
H_u	1	0	$2_{1/2}$
H_d	1	0	$2_{-1/2}$
H'_u	1	0	$2_{1/2}$
H'_d	1	0	$2_{-1/2}$
S	1	3	1
\bar{S}	1	-3	1
q	3	0	$2_{1/6}$
t^c	$\bar{3}$	0	$1_{-2/3}$
b^c	$\bar{3}$	0	$1_{1/3}$

$$\left(H'_u H'_d - S \bar{S} = \frac{\Lambda'^2}{(4\pi)^2} \right)$$

gauged $\langle H' \rangle = 0$
 $\langle S \rangle \neq 0$
 at SUSY level.

S is not dynamical
 one can integrate them out.

arriving at the MSSM-like model

$$W = \frac{\lambda_u \Lambda'}{4\pi} H_u H'_d + \frac{\lambda_d \Lambda'}{4\pi} H_d H'_u - \frac{\lambda_q \lambda_t}{4\pi} H'_u t^c q - \frac{\lambda_q \lambda_b}{4\pi} H'_d b^c q.$$

$$K \ni \frac{\Lambda'^{\dagger}}{\Lambda'} H'_u H'_d + \text{h.c.}$$

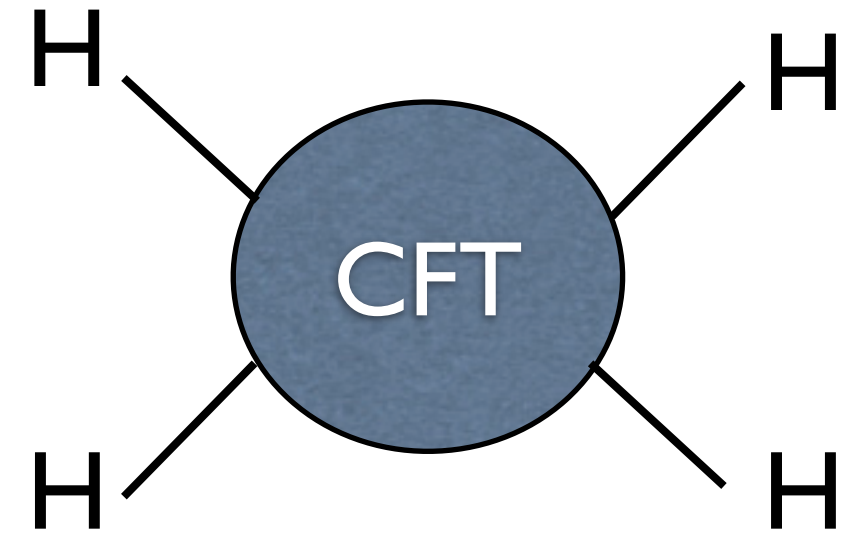
μ -like terms

obtained from kinetic terms for S and \bar{S} .

We consider SUSY breaking by turning on

$$\Lambda'(1 + m_{\text{SUSY}}\theta^2) \quad \text{with} \quad m_{\text{SUSY}} \sim \Lambda' \sim 1 \text{ TeV}$$

Higgs potential



$$V \ni \frac{m_{\text{SUSY}}^2}{(4\pi)^2} (|\lambda_u H_u|^2 + |\lambda_d H_d|^2) + \frac{1}{(4\pi)^2} (|\lambda_u H_u|^4 + |\lambda_d H_d|^4).$$

$$V \ni m_{\text{SUSY}}^2 (|H'_u|^2 + |H'_d|^2) + \dots$$

H_d is the main Higgs direction

$$V \ni m_{\text{SUSY}} \left(\frac{\lambda_u \Lambda'}{4\pi} H_u H'_d + \frac{\lambda_d \Lambda'}{4\pi} H_d H'_u + \text{h.c.} \right),$$

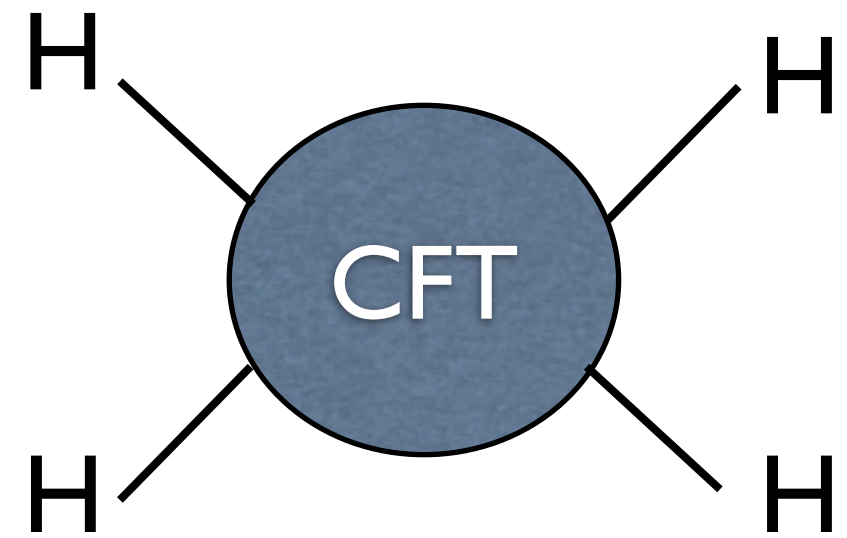
$$W \ni \frac{\Lambda'}{4\pi} (\lambda_u H_u H'_d + \lambda_d H_d H'_u) + m_{\text{SUSY}} H'_u H'_d.$$

H' are heavy

$$V \ni m_{\text{SUSY}}^2 H'_u H'_d + \text{h.c.}$$

Partially composite Higgs
[RK, Luty, Nakai '12]

$$m_h = 126 \text{ GeV}$$



Higgs quartic term:

$$\frac{\lambda_d^4}{(4\pi)^2} + \frac{g_L^2 + g_Y^2}{2} \sim \frac{m_h^2}{\langle H \rangle^2} \sim 0.5, \quad \frac{\lambda_d}{4\pi} \sim 0.2.$$

not bad.

tuning: required size of the Higgs quadratic terms

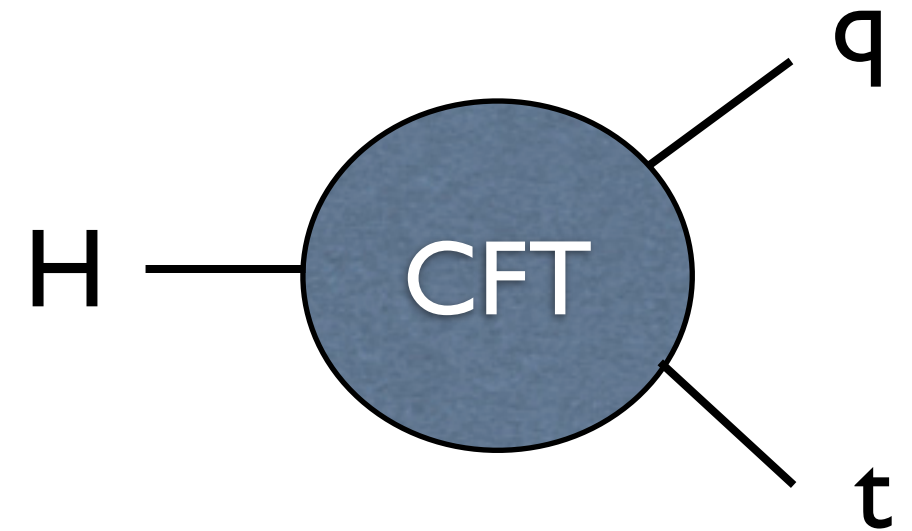
$$\delta = \frac{m_h^2/2}{(\lambda_d m_{\text{SUSY}}/4\pi)^2} = 20\% \cdot \left(\frac{m_{\text{SUSY}}}{1 \text{ TeV}} \right)^{-2} \left(\frac{\lambda_d/4\pi}{0.2} \right)^{-2}.$$

typical size

not bad.

fixed point values: $\frac{\tilde{g}}{4\pi} \sim 0.41, \quad \frac{\lambda_d}{4\pi} \sim 0.11, \quad \frac{\lambda_u}{4\pi} \sim 0.26, \quad \frac{\lambda_t}{4\pi} \sim 0.29, \quad \frac{\lambda_q}{4\pi} \sim 0.26,$

top mass



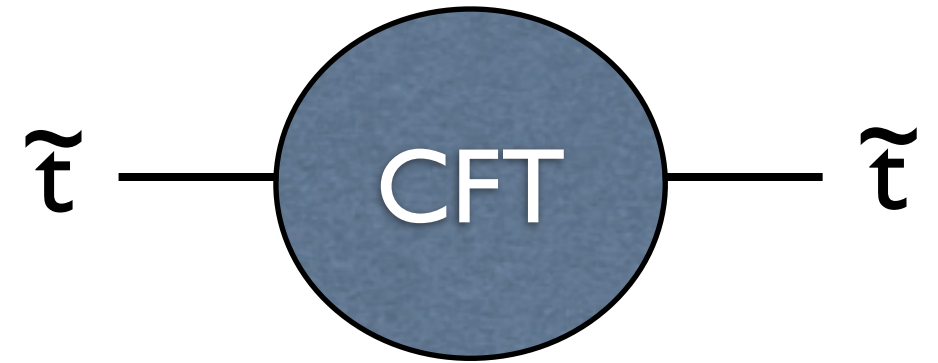
$$K \ni \frac{\lambda_q \lambda_t \lambda_d}{(4\pi)^2} \frac{1}{\Lambda'^{\dagger}} H_d^{\dagger} t^c q, \quad W \ni -\frac{\lambda_q \lambda_t}{4\pi} H'_u t^c q.$$

$$\longrightarrow m_t \sim \frac{\lambda_q \lambda_t \lambda_d}{(4\pi)^2} \langle H_d \rangle \sim 160 \text{ GeV} \cdot \left(\frac{\lambda_d/4\pi}{0.2} \right) \left(\frac{\lambda_q/4\pi}{0.6} \right) \left(\frac{\lambda_t/4\pi}{0.6} \right).$$

not bad.

note: top obtains a mass from H_d

fixed point values: $\frac{\tilde{g}}{4\pi} \sim 0.41, \quad \frac{\lambda_d}{4\pi} \sim 0.11, \quad \frac{\lambda_u}{4\pi} \sim 0.26, \quad \frac{\lambda_t}{4\pi} \sim 0.29, \quad \frac{\lambda_q}{4\pi} \sim 0.26,$

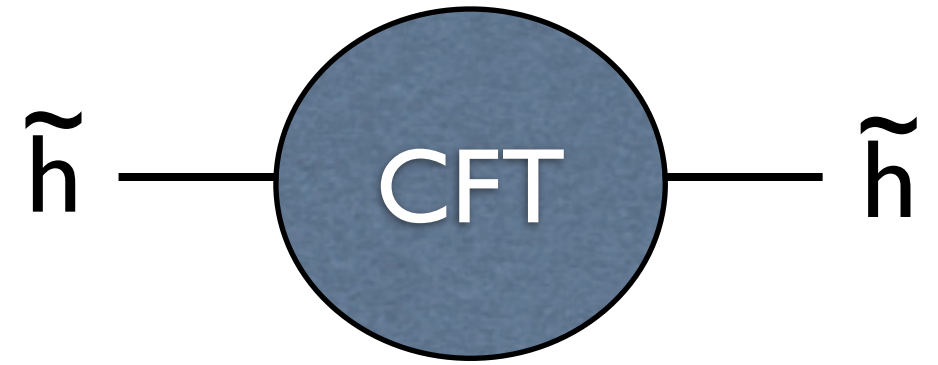


stop/sbottom

$$m_{\tilde{t}} \sim m_{\tilde{b}} \sim \frac{\lambda_q}{4\pi} m_{\text{SUSY}} \sim 600 \text{ GeV} \cdot \left(\frac{\lambda_q/4\pi}{0.6} \right) \left(\frac{m_{\text{SUSY}}}{1 \text{ TeV}} \right).$$

should be observed soon!
(should have been observed?)

fixed point values: $\frac{\tilde{g}}{4\pi} \sim 0.41$, $\frac{\lambda_d}{4\pi} \sim 0.11$, $\frac{\lambda_u}{4\pi} \sim 0.26$, $\frac{\lambda_t}{4\pi} \sim 0.29$, $\frac{\lambda_q}{4\pi} \sim 0.26$,



Higgsino

$$m_{\tilde{h}} \sim \frac{\lambda_u \lambda_d}{(4\pi)^2} \frac{\Lambda'^2}{m_{\text{SUSY}}} \sim 120 \text{ GeV} \cdot \left(\frac{\lambda_d/4\pi}{0.2} \right) \left(\frac{\lambda_u/4\pi}{0.6} \right) \left(\frac{\Lambda'}{1 \text{ TeV}} \right)^2 \left(\frac{m_{\text{SUSY}}}{1 \text{ TeV}} \right)^{-1}.$$

pretty light.

fixed point values: $\frac{\tilde{g}}{4\pi} \sim 0.41$, $\frac{\lambda_d}{4\pi} \sim 0.11$, $\frac{\lambda_u}{4\pi} \sim 0.26$, $\frac{\lambda_t}{4\pi} \sim 0.29$, $\frac{\lambda_q}{4\pi} \sim 0.26$,

dynamical sector

$$\Lambda' \sim 1 \text{ TeV}$$

We can access to UV dynamics of QCD.

We expect ρ -like resonances (W' , Z')

very interesting.

We saw that

EWSB may be a **magnetic** description
of higher dim. QCD.



Can we also understand confinement/chiral symmetry
breaking in QCD as the Higgs mechanism
in the **magnetic** picture?

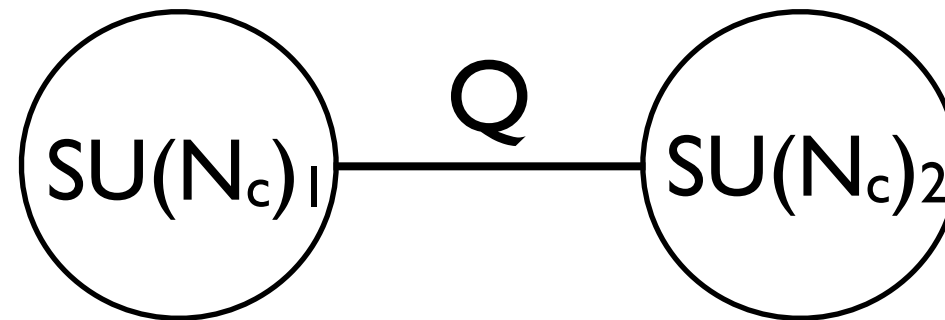
[Mandelstam '75, 't Hooft '75]

Maybe deconstruction and duality in SUSY theories
can provides us with a new insight.

Regulating QCD to higher dimensional SQCD

N_f quarks

[RK '11][RK,Yokoi '14]

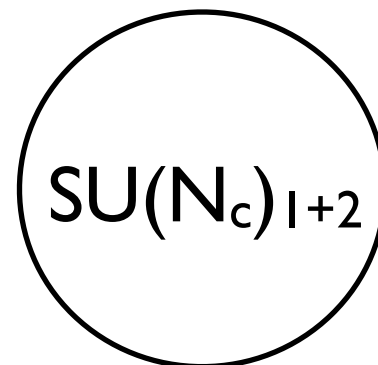


$(N_f < N_c)$

This provides an interesting deformation of QCD.

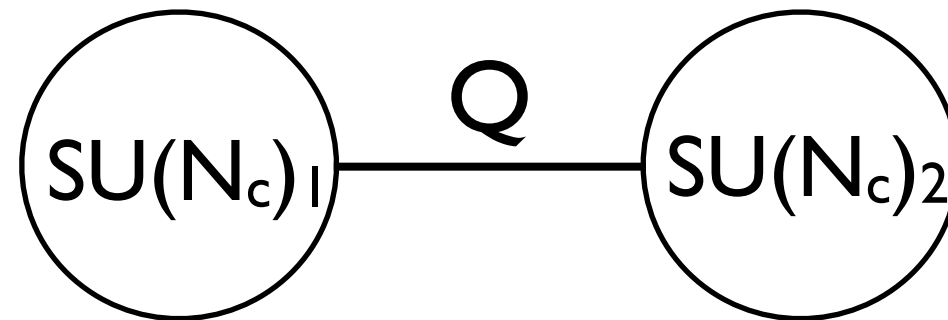
For $v \gg \Lambda_1, \Lambda_2$, this is just QCD.

N_f quarks



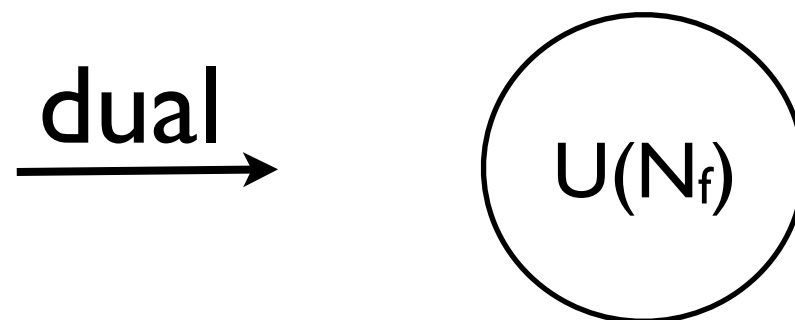
$$\Lambda_1 \gg \Lambda_2 \gg v$$

N_f quarks



Starting with $N=2$ SUSY and
adding a small breaking of $N=2$ SUSY to $N=1$

N_f dual quarks



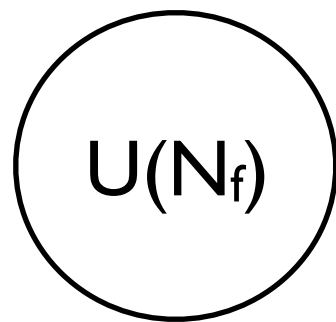
magnetic picture

color-flavor locking

[See also Shifman and Yung '07, ...]

N_f dual quarks

turning on v



$$\langle q \rangle = \langle \bar{q} \rangle = \begin{pmatrix} v/\sqrt{N_c} & & \\ & \ddots & \\ & & v/\sqrt{N_c} \end{pmatrix}$$

magnetic gauge bosons of $U(N_f)$ behave
as **vector mesons** ρ and ω .

string formation from $U(1)$ breaking \longrightarrow **confinement**
[Mandelstam '75, 't Hooft '75]

low energy QCD as magnetic picture?

N=0?

Seiberg duality + soft SUSY breaking terms

electric

	$SU(N_c)$	$SU(N_f)_L$	$SU(N_f)_R$	$U(1)_B$	$SU(N_c)_V$	$U(1)_{B'}$	$U(1)_R$
Q	N_c	N_f	1	1	1	0	$(N_f - N_c)/N_f$
\bar{Q}	\bar{N}_c	1	\bar{N}_f	-1	1	0	$(N_f - N_c)/N_f$
Q'	N_c	1	1	0	\bar{N}_c	1	1
\bar{Q}'	\bar{N}_c	1	1	0	N_c	-1	1

Table 1: Quantum numbers in the electric picture.

magnetic

	$SU(N_f)$	$SU(N_f)_L$	$SU(N_f)_R$	$U(1)_B$	$SU(N_c)_V$	$U(1)_{B'}$	$U(1)_R$
q	N_f	\bar{N}_f	1	0	1	N_c/N_f	N_c/N_f
\bar{q}	\bar{N}_f	1	N_f	0	1	$-N_c/N_f$	N_c/N_f
Φ	1	N_f	\bar{N}_f	0	1	0	$2(N_f - N_c)/N_f$
q'	N_f	1	1	1	N_c	$-1 + N_c/N_f$	0
\bar{q}'	\bar{N}_f	1	1	-1	\bar{N}_c	$1 - N_c/N_f$	0
Y	1	1	1	0	1 + Adj.	0	2
Z	1	1	\bar{N}_f	-1	\bar{N}_c	1	$(2N_f - N_c)/N_f$
\bar{Z}	1	N_f	1	1	N_c	-1	$(2N_f - N_c)/N_f$

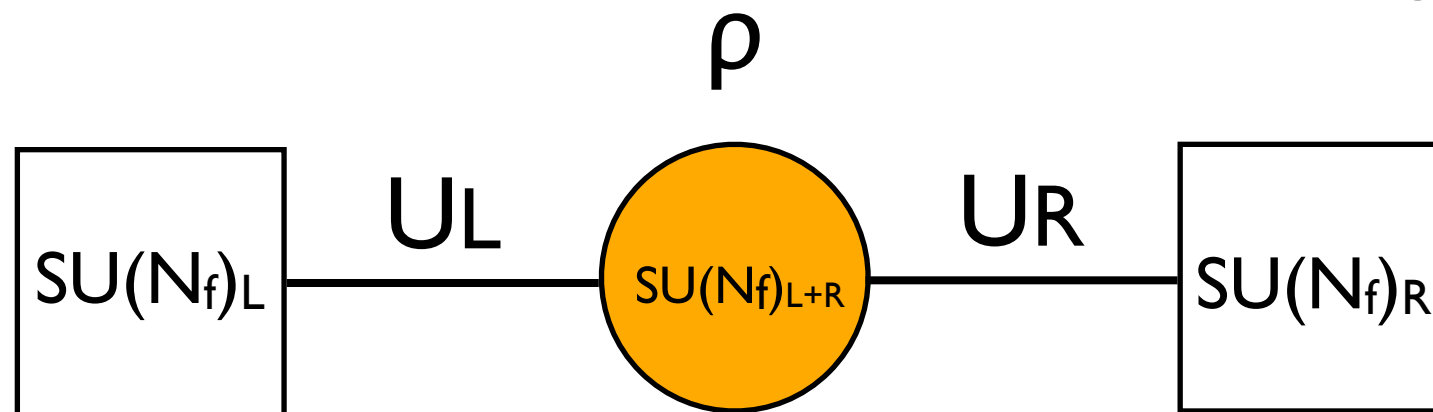
Tachyonic

One can also see the Color-Flavor Locking.

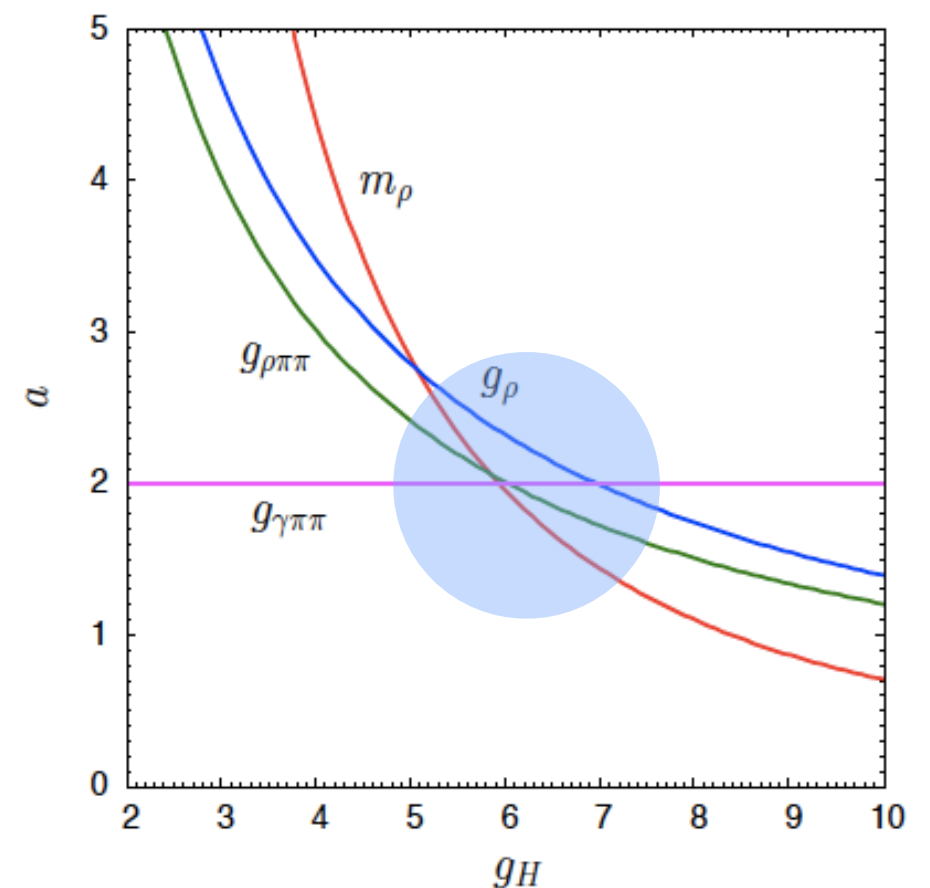
May not be totally crazy.

Hidden Local Symmetry

[Bando, Kugo, Uehara, Yamawaki, Yanagida '85]



$$\begin{aligned} \mathcal{L} = & -\frac{1}{4g_H^2} F_{\mu\nu}^a F^{a\mu\nu} \\ & + \frac{af_\pi^2}{2} \text{tr} [|D_\mu U_L|^2 + |D_\mu U_R|^2] \\ & + \frac{(1-a)f_\pi^2}{4} \text{tr} [|\partial_\mu (U_L U_R)|^2] . \end{aligned}$$



We see such a picture in the real world.

Quiver deformation provides us with
an understanding of **HLS as
the magnetic gauge theory.**

weak coupling \longleftrightarrow strong coupling

QCD

HLS as
magnetic theory

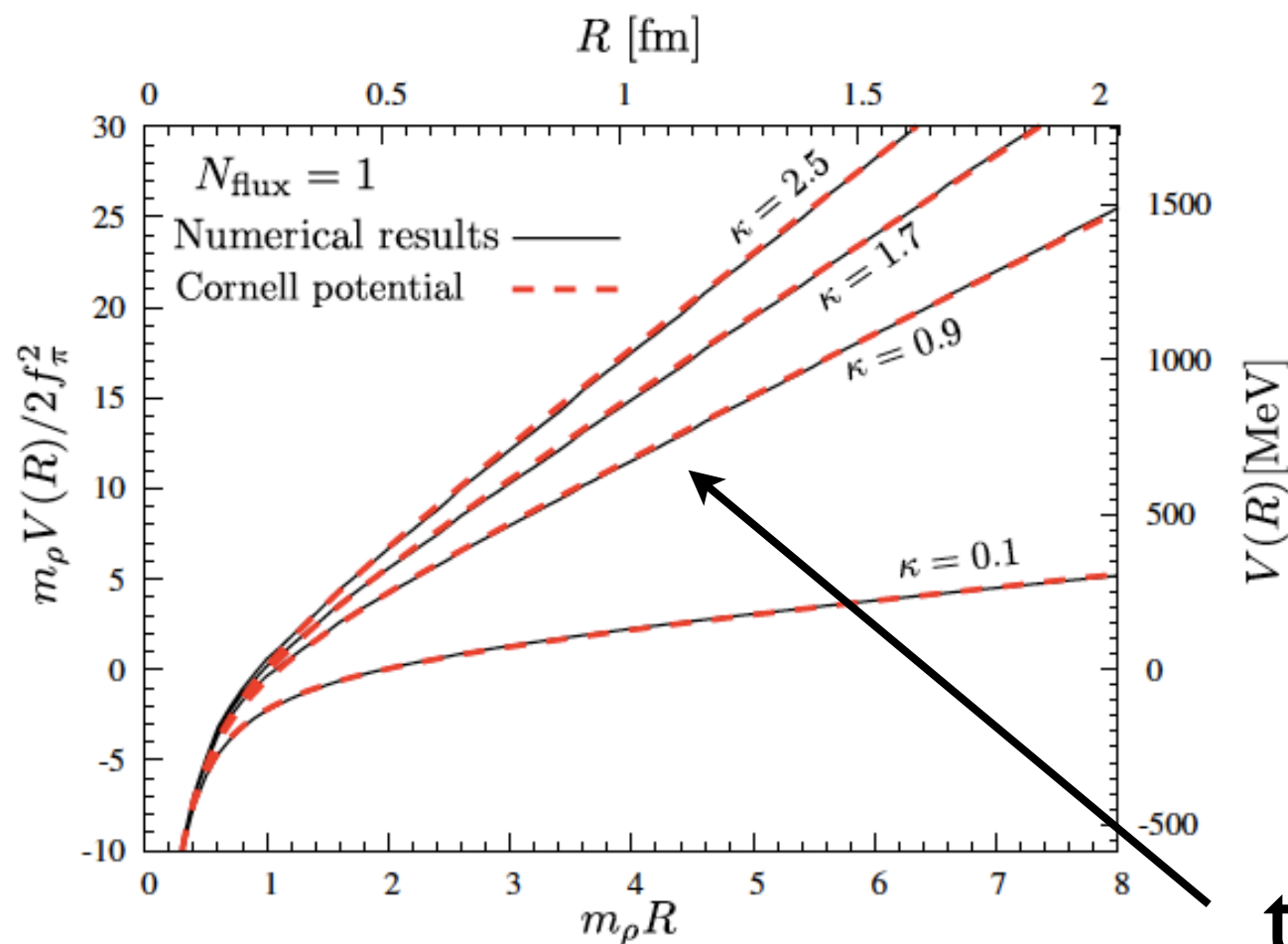
large extra dim. \longleftrightarrow small extra dim.

See also

[Seiberg '95, Harada, Yamawaki '99, Komargodski '10, RK '11, Abel, Barnard '12]

Moreover,

one can construct a string configuration made of ρ , ω , and f_0 and calculate an energy.



$$g_\rho = (340 \text{ MeV})^2,$$

$$m_\rho = 770 \text{ MeV},$$

$$\sim m_\omega$$

$$m_S = m_A = 980 \text{ MeV},$$

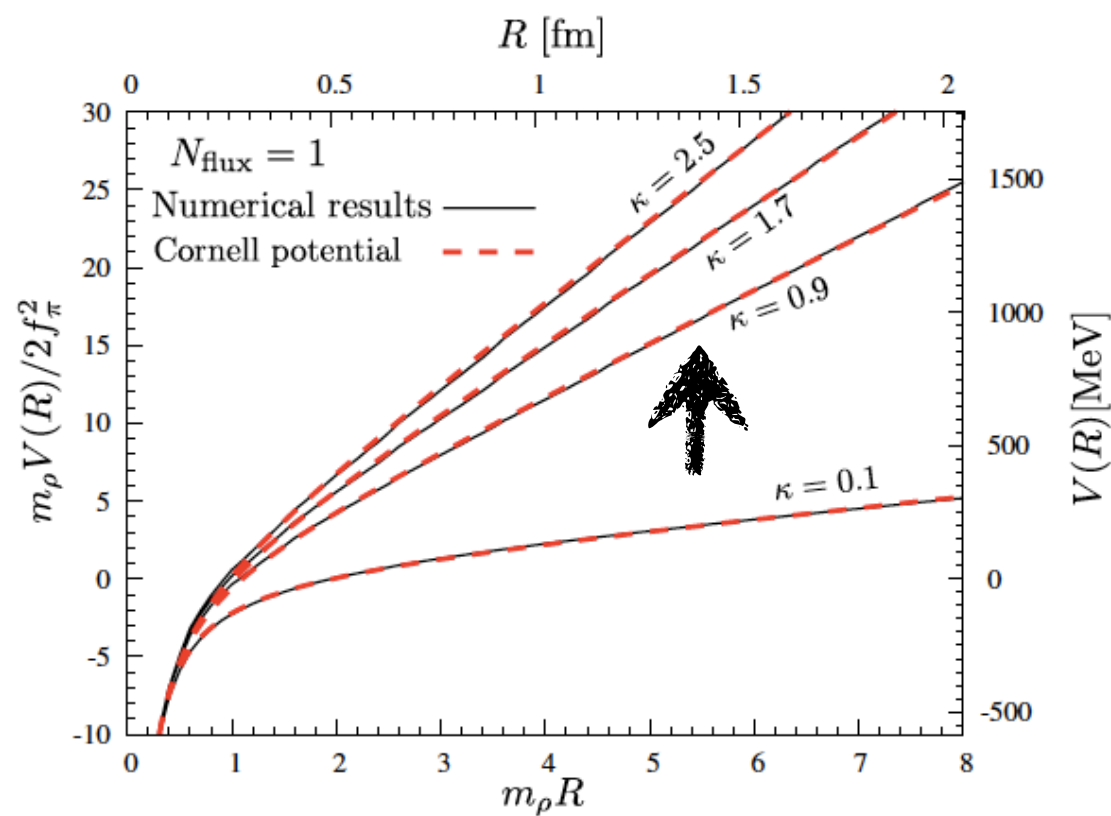
(scalar meson masses)

this line

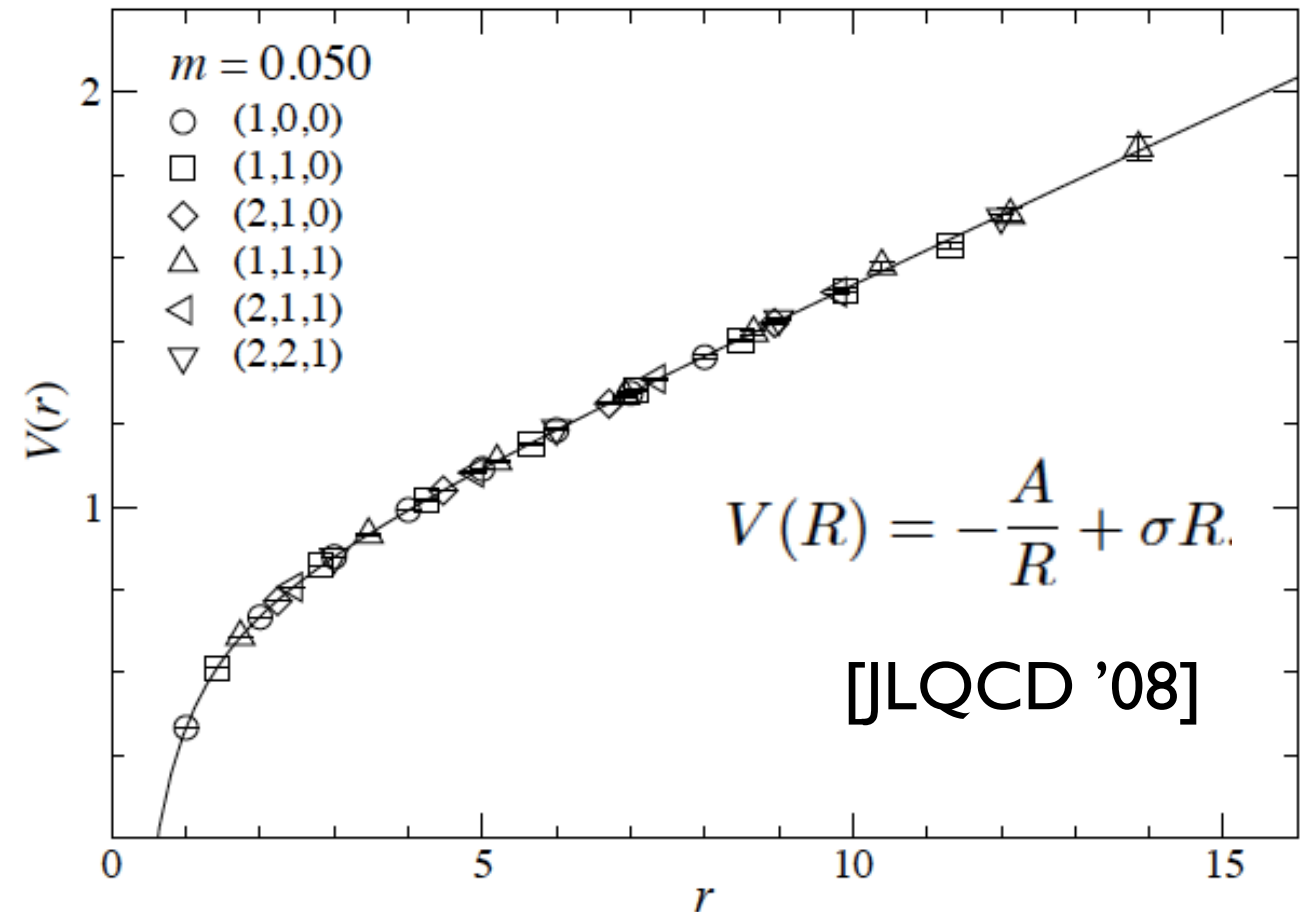
$$V(R) = -\frac{A}{R} + \sigma R.$$

$$A = 0.25 \quad \sqrt{\sigma} = 400 \text{ MeV}$$

Comparing to lattice QCD



$$A = 0.25 \quad \sqrt{\sigma} = 400 \text{ MeV}$$



$$A \sim 0.25 - 0.5, \quad \sqrt{\sigma} \sim 430 \text{ MeV}.$$

pretty consistent.

confining string $\stackrel{?}{=}$ hadron vortex

Summary

- We studied a quiver model for EWSB. The Higgs fields **emerge as magnetic degrees of freedom**. By adding SUSY breaking terms, EWSB can occur while 126 GeV Higgs boson is naturally explained.
- Confinement and Chiral Symmetry Breaking in QCD may also have a picture of the Higgs mechanism via duality.